

# 1.7 Negative exponents

key

## ACTIVITY 1 Negative exponents

When the base  $a$  is a non-zero real number and  $n$  is a natural number,  $a^{-n}$  is a negative power defined by  $a^{-n} = \frac{1}{a^n}$ .

Calculate.

a)  $3^{-2} = \frac{1}{3^2}$       b)  $(-5)^{-2} = \frac{1}{(-5)^2}$  or  $\frac{1}{25}$       c)  $-5^{-2} = -\frac{1}{5^2}$  or  $-\frac{1}{25}$   
 d)  $(-2)^{-3} = \frac{1}{(-2)^3}$       e)  $10^{-4} = \frac{1}{10^4}$       f)  $\left(\frac{2}{3}\right)^{-2} = \frac{2^{-2}}{3^{-2}} = \frac{3^2}{2^2}$   
 g)  $(0.2)^{-1} = \frac{1}{0.2} = 5$       h)  $(0.05)^{-3} = \left(\frac{1}{20}\right)^{-3} = 20^3$       i)  $(0.01)^{-2} = \frac{1}{100}$  or  $10^{-2}$

$\left(\frac{1}{5}\right)^{-1} = 5$

### NEGATIVE EXPONENTS

For any non-zero real number  $a$ , and any natural number  $n$ , we have:

$$a^{-n} = \frac{1}{a^n}$$

Ex.:  $5^{-2} = \frac{1}{5^2} = \frac{1}{25}$ ,       $(-4)^{-2} = \frac{1}{(-4)^2} = \frac{1}{16}$ ,       $(-2)^{-3} = \frac{1}{(-2)^3} = \frac{-1}{8}$ .

1. Explain why it is necessary for the base  $a$  to be non-zero in the expression  $a^{-n}$ .

2. The laws of exponents (section 1.6) remain valid when the exponents are negative. Simplify the following calculations using the appropriate law of exponents.

a)  $2^3 \times 2^{-5}$

$2^{3+(-5)} = 2^{-2} \rightarrow \frac{1}{2^2} = \frac{1}{4}$

c)  $(x^2y^{-3})^{-2}$

$x^{-4}y^6 \rightarrow \frac{y^6}{x^4}$

e)  $\left(\frac{3a^{-2}}{b^4}\right)^{-2}$

$\frac{3^2 a^4}{b^{-8}} = \frac{9a^4}{b^8}$

b)  $(2^2)^{-3}$

$2^{-6} \rightarrow \frac{1}{2^6}$

d)  $\left(\frac{x^{-3}}{y^2}\right)^{-2}$

$\frac{x^6}{y^{-4}} = \frac{x^6 y^4}{1}$

$\left(\frac{y^2}{x^{-3}}\right)^2 = \frac{y^4}{x^{-6}} = x^6 y^4$

~~Assignment~~

Date \_\_\_\_\_

Period \_\_\_\_\_

Simplify. Your answer should contain only positive exponents.

Key

1)  $u^{-2} \cdot 3u^{-4}v^2$

$$3u^{-6}v^2 \rightarrow \frac{3v^2}{u^6}$$

3)  $2x^3y^3 \cdot y^4 \cdot 3y^4$

$$6x^3y^{11}$$

5)  $x^2y^{-2} \cdot 4x^4y^3$

$$4x^6y^1$$

7)  $x^0 \cdot 4x^4y^2$

$$4x^4y^2$$

9)  $y^{-4}x^4$

$$\frac{x^4}{y^4}$$

11)  $x^4y^{-4} \cdot x^{-2}y^4$

$$x^2$$

13)  $uv^3 \cdot u^4v^0$

$$u^5v^3$$

15)  $2xy^{-4} \cdot yx^3$

$$2x^4y^{-3} \rightarrow \frac{2x^4}{y^3}$$

17)  $2x^4y^4 \cdot 2x^{-1}$

$$4x^3y^4$$

19)  $2b^{-3} \cdot 2a^{-2}b^{-2}$

$$4ab^{-5} \rightarrow \frac{4}{a^2b^5}$$

2)  $2y^{-3} \cdot x^2 \cdot 2x^{-2}$

$$4y^{-3} \rightarrow \frac{4}{y^3}$$

4)  $4a^2b^2 \cdot 3ab$

$$12a^3b^3$$

6)  $2a^{-4} \cdot 4ab^{-2}$

$$8a^{-3}b^{-2} \rightarrow \frac{8}{a^3b^2}$$

8)  $a^{-1}b^0 \cdot 4a^{-3}b^{-4}$

$$4a^{-4}b^{-4} \rightarrow \frac{4}{a^4b^4}$$

10)  $2m^2n^{-3} \cdot 2m^3n^{-1} \cdot 4m^4n^{-1}$

$$16m^9n^{-5} \rightarrow \frac{16m^9}{n^5}$$

12)  $m^3 \cdot m^{-1}n^0$

$$m^2$$

14)  $x^4y^{-3} \cdot xy^{-1}$

$$x^5y^{-4} \rightarrow \frac{x^5}{y^4}$$

16)  $4u^3v^{-3} \cdot 2uv^{-4} \cdot 2u^2v^{-4}$

$$16u^6v^{-11} \rightarrow \frac{16u^6}{v^{11}}$$

18)  $2x^{-4} \cdot 2x^{-3}y^4$

$$4x^{-7}y^4 \rightarrow \frac{4y^4}{x^7}$$

20)  $a^2b^4 \cdot 2a^0$

$$2a^2b^4$$